

## Interest

P: Principal (\$)I: Interest (\$)A: final, total Amount (\$) (note that  $A = P + I$ )t: time (years)r: annual interest rate (as a decimal)n: the number of times the interest is compounded per year(Note:  $e$  is a constant, approximately 2.71828)

<u>Simple Interest</u>	$I = P * r * t$ $A = P(1 + rt)$
<u>Compounded Interest</u>	$A = P \left(1 + \frac{r}{n}\right)^{nt}$
<u>Continuously Compounded Interest</u>	$A = Pe^{rt}$

**Note:** the value of  $n$  is often determined by the frequency word used.

Yearly (annually): $n = 1$	Semi-annually: $n = 2$
Quarterly: $n = 4$	Bi-weekly: $n = 26$
Weekly: $n = 52$	Daily: $n = 365$

**Example:** Bobby wants to borrow \$100,000 to buy a house. How much will he pay in total for a 20-year loan if the 4% interest is computed as:

a) simple interest; b) compounded monthly; c) compounded continuously?

Based on the wording:  $P = \$100,000$   $r = 0.04$  (4% as a decimal)  $t = 20$   $n = 12$

a) Simple Interest:  $A = P(1 + rt)$   
 $= \$100,000(1 + 0.04 * 20) = \$180,000$

b) Compounded Monthly:  $A = P \left(1 + \frac{r}{n}\right)^{nt}$   
 $= \$100,000 \left(1 + \frac{0.04}{12}\right)^{20 * 12} = \$222,258.21$

c) Compounded Continuously:  $A = Pe^{rt}$   
 $= \$100,000 * e^{0.04 * 20} = \$222,554.09$