## PROPERTIES OF LOGARITHMS

In the list that follows, $a, b, M, N$ and $r$ are real numbers.
Also, $a>0, a \neq 1, b>0, b \neq 1, M>0$, and $N>0$

- Definition:

$$
y=\log _{a} x \leftrightarrow x=a^{y}
$$

" $\leftrightarrow$ " means the statements are equivalent. The log base $a$ of $x$ is the power that $a$ needs to be raised to, to get $x$.

- Properties of Logarithms:

| $\log _{a} 1=0$ |
| :---: |
| $\log _{a} a=1 ; \ln e=1$ |
| $a^{\log _{a} M}=M ; \log _{a} a^{r}=r$ |
| $\log _{a}(M N)=\log _{a} M+\log _{a} N$ |
| $\log _{a} \frac{M}{N}=\log _{a} M-\log _{a} N$ |
| $\log _{a} M^{r}=r \log _{a} M$ |
| If $M=N$, then $\log _{a} M=\log _{a} N$ |
| If $\log _{a} M=\log _{a} N$, then $M=N$ |

- Change-of-base Formula:

$$
\log _{a} M=\frac{\log _{b} M}{\log _{b} a}
$$

For a more detailed discussion of logarithms, including practice problems, click here.

